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# ON THE CHOICE OF DIHEDRAL ANGLE POTENTIAL ENERGY FUNCTIONS FOR *n*-ALKANES

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The parameters of the GROMOS96 force field governing dihedral angle transitions in aliphatic chains have been reconsidered, since these parameters produce a too large ratio of *trans* to *gauche* conformations in such chains. A refined set of parameters for dihedral angle interactions and third-neighbour interactions involving CH<sub>2</sub> and CH<sub>3</sub> atoms is proposed. They were obtained by fitting to the heat of vaporization, pressure and *trans-gauche* ratio for liquids of three *n*-alkanes, *n*-butane, *n*-pentane and *n*-hexane. The new parameter set does reproduce better these quantities and should therefore be more appropriate for use in simulations of polymers and membranes. A comparison of the mentioned properties obtained from simulations with united-atom models and from simulations with an all-atom model shows that the latter does not necessarily yield an improved description of molecular behaviour.

*Keywords:* *n*-Alkanes; force field parameters; GROMOS force field; molecular dynamics simulation; *trans-gauche* energy differences

## 1. INTRODUCTION

The practical value of computer simulation of molecular systems relies very much on the accuracy of the potential energy function or force field that is used. For biomolecular systems a number of force fields have been developed and refined during the past decades, and are widely used [1–13, 50]. The potential energy functions of different force fields have slightly different forms, and the force field parameters are generally obtained by fitting of a range of molecular properties against different sets of quantum-mechanical

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and experimental data regarding small molecules. A force field can be tested by application to biomolecular systems for which structural, energetic and dynamic data are available.

When using the most recent version of the GROMOS (Groningen Molecular Simulation) force field [11, 14, 15] in simulations of membranes, which involve – in contrast to proteins, sugars and nucleotides – long aliphatic carbon chains, we observed that the GROMOS96 43A1 force field [11] favours too strongly *trans* over *gauche* conformations in aliphatic chains. In the parametrisation of the GROMOS 43A1 force field, the  $\text{CH}_1$ ,  $\text{CH}_2$  and  $\text{CH}_3$  united-atom van der Waals interaction parameters had been determined such that the energy (heat of vaporization) and density of a number of *n*-alkanes in the liquid phase was reproduced [14]. The parameters of the torsional angle term in the force field had not been changed from the previous force field version [16]. Thus, these could be varied to obtain values for which a correct *trans-gauche* ratio is obtained, while still maintaining the correct energy and density of the *n*-alkane liquids.

We report a refinement of the parameters for aliphatic chains in the GROMOS 43A1 force field. The experimental and quantum-mechanically calculated data used in the parametrisation are considered, and a comparison of the properties of the *n*-alkanes butane, pentane and hexane obtained using various parameter sets and also using OPLS parameters [12, 13] is presented. The effects of using different cut-off radii for the intermolecular non-bonded interactions is considered in an appendix.

## 2. SELECTION OF TARGET VALUES FOR THE PARAMETRISATION

First, the target values to be used in the parametrisation have to be chosen. As target values for the heat of vaporization  $\Delta H_{\text{vap}}$  and the pressure  $p$  (for a given density) for *n*-butane, *n*-pentane and *n*-hexane were taken experimental values for these quantities [17], as in [14]. To select a target value for the ratio of *trans* to *gauche* conformations or for the *gauche-trans* energy difference, values obtained by spectroscopic measurements or by quantum-theoretical model calculations were considered. Over several decades, a range of experimental and theoretical values has been published, as is illustrated for *n*-butane in Figure 1. The most recent data seem to converge around  $2.7 \text{ kJ} \cdot \text{mol}^{-1}$ . We have chosen the average of the encircled data points as target value for the *n*-butane *gauche-trans* energy difference:  $2.66 \pm 0.16 \text{ kJ} \cdot \text{mol}^{-1}$ . A similar procedure was followed to select the target *gauche-trans* difference  $E_g - E_t$  for *n*-pentane and *n*-hexane, see Table I.

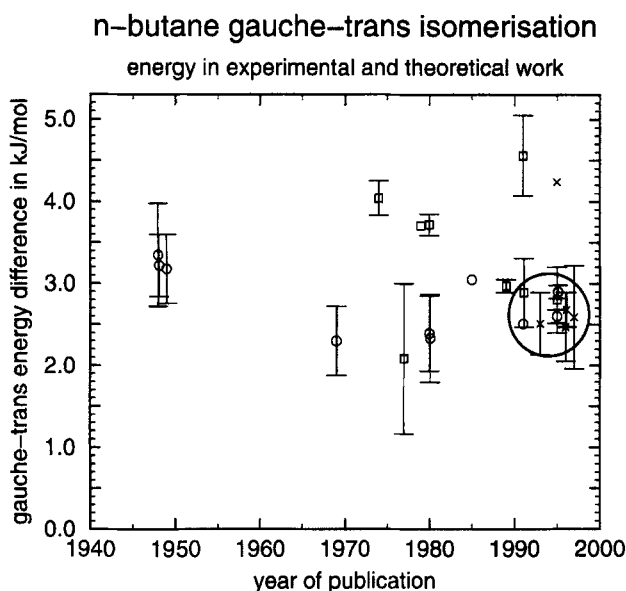


FIGURE 1 Over several decades, *n*-butane *gauche*–*trans* energy difference was measured in the liquid phase (circles), gas phase (squares) and calculated by high-level *ab initio* methods (crosses). Error bars are shown whenever the data was available. The average of the encircled data was chosen as target value for the aliphatic GROMOS force field parameters. It amounts to  $2.66 \pm 0.16$  kJ/mol. References for the data and experimental methods are found in [18] to [36].

TABLE I Target value determination for energy differences between different conformations of *n*-alkanes. The relative potential energies *E* are indicated through their differences by letters *g* for the *gauche* and *t* for the *trans* conformation and both letters for the barriers between the two conformations. The sources of data are shown by reference number. If more than one reference is given, the average was taken even if different methods or molecules of similar dihedral properties were involved. In the case of *n*-pentane some low-level *ab-initio* calculations have been made (result section, Fig. 2)

Molecule	$E_{poi}$	References	Target value [kJ/mol]
<i>n</i> -Butane	$E_g - E_t$	[29, 31, 32, 33, 35, 36]	$2.66 \pm 0.16^*$
	$E_{tg} - E_t$	[35]	$13.85 \pm 0.42^{\ddagger}$
	$E_{gg} - E_t$	[35]	$22.93 \pm 2.09^{\ddagger}$
<i>n</i> -Pentane	$E_g - E_t$	[19, 24, 29, 32, 37, 38, 39, 40]	$2.26 \pm 0.25^{\S}$
	$E_{tg} - E_t$	–	–
	$E_{gg} - E_t$	–	–
<i>n</i> -Hexane	$E_g - E_t$	[35, 41]	$2.14 \pm 0.16^{\#}$
	$E_{tg} - E_t$	[35]	$11.76 \pm 0.42^{\ddagger}$
	$E_{gg} - E_t$	[35]	$21.67 \pm 0.42^{\ddagger}$

\* average over several methods,

<sup>†</sup> best available *ab-initio* level result,

<sup>‡</sup> average over all data and

<sup>#</sup> average over larger molecules.

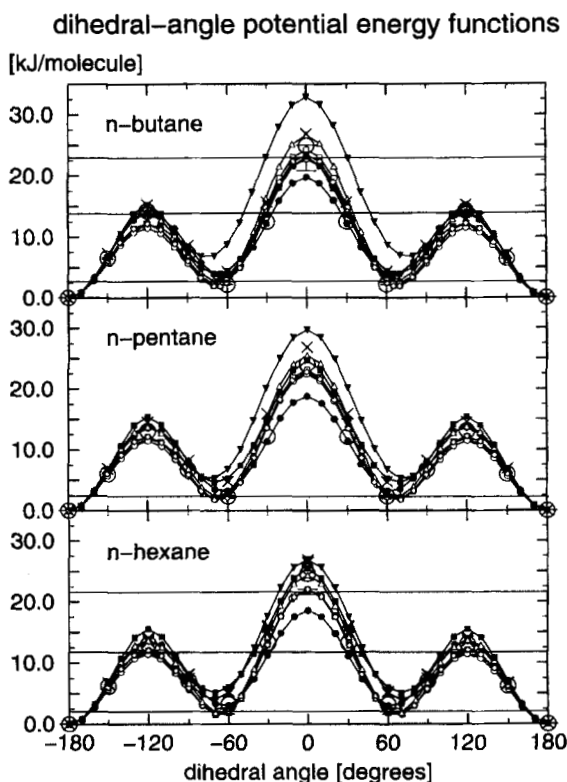


FIGURE 2 The original GROMOS96 potential energy as function of dihedral angle value for *n*-butane, *n*-pentane and *n*-hexane is shown as eyeguiding line with filled triangles. Target energy values derived from experimental or theoretical work (Tab. I) are indicated with horizontal lines.

The modifications of the GROMOS96 force field, in which the third-neighbour van der Waals repulsive ( $CS_{12}$ ) parameter was reduced and the force constant ( $K_{\varphi_n}$ ) for alkane dihedral angle potentials was increased (Tab. II), are shown as eyeguiding lines with open white triangles (a), squares (b), circles (c) or diamonds (d).

The result for the OPLS united- and all-atom force fields were obtained using a modified version of the GROMOS96 software (for all-atom electrostatic 1-4 scaling). The results are shown as filled circles (united-atom) or filled squares (all-atom) including an eyeguiding line.

Additional values illustrated are: Hartree Fock for several basis sets (up to 6-31G\*\*, large crosses) and MP2 6-31G\*\* (large circles).

Literature values from high-level *ab-initio* quantum calculations were used to obtain target values for the energy difference  $E_{tg} - E_t$  between the *trans/gauche* barrier and the *trans* conformation, and for the energy difference  $E_{gg} - E_t$  between the *gauche/gauche* or *cis* barrier and the *trans* conformation, see Table I.

### 3. MODEL CALCULATIONS AND SIMULATIONS

The functional form of the GROMOS96 force field has been given in Refs. [11, 14, 15, 42]. The terms representing torsional interactions and non-bonded interactions are

$$V^{\text{trig}}(\vec{r}) = \sum_{n=1}^{N_\varphi} K_{\varphi_n} [1 + \cos(\delta_n) \cos(m_n \varphi_n(\vec{r}))] \quad (1)$$

and

$$V^{\text{nonb}}(\vec{r}) = \sum_{\substack{\text{non-bonded} \\ \text{pairs } (i,j)}} \left[ \frac{C_{12}(i,j)}{r_{ij}^6} - C_6(i,j) \right] \frac{1}{r_{ij}^6} \\ + \sum_{\substack{\text{non-bonded} \\ \text{pairs } (i,j)}} \frac{q_i q_j}{4\pi\epsilon_0\epsilon_1} \left[ \frac{1}{r_{ij}} - \frac{C_{rf} r_{ij}^2}{2R_{rf}^3} - \frac{1 - (1/2)C_{rf}}{R_{rf}} \right] \quad (2)$$

The summation in (1) runs over the  $N_\varphi$  dihedral or torsional angles  $\varphi_n(\vec{r})$  in the molecules, which depend on the Cartesian coordinates  $\vec{r}$  of the atoms in the system. The parameters of the torsional interaction term for dihedral angle  $\varphi_n$  are the force constant  $K_{\varphi_n}$ , phase shift  $\delta_n$  and multiplicity  $m_n$ . The summation over the non-bonded pairs  $(i, j)$  requires some clarification. No non-bonded interaction is calculated for atom pairs that are connected by one or two bonds (or in special cases not considered here, three bonds) and slightly weaker van der Waals interactions are used for certain atom types, e.g., the aliphatic CH<sub>1</sub>, CH<sub>2</sub> and CH<sub>3</sub> united atoms considered here, separated by three bonds. These are called third-neighbour or 1–4 van der Waals interactions and parameters ( $CS_{12}(i, j)$  and  $CS_6(i, j)$  replacing  $C_{12}(i, j)$  and  $C_6(i, j)$  in (2)). The distance between atoms  $i$  and  $j$  is indicated by  $r_{ij}$ . The second term in (2), Coulomb plus reaction field, only applies when the atoms carry non-zero partial charges  $q_i$ . For aliphatic carbons in the GROMOS and OPLS *united-atom* force fields these charges are zero. In the calculations using the OPLS all-atom force field, we used a dielectric permittivity of 1 ( $\epsilon_1 = \epsilon_2 = 1.0$ ) both inside ( $\epsilon_1$ ) and outside ( $\epsilon_2$ ) the long-range cut-off radius  $R_{rf} = 1.4$  nm. Since the ionic strength of the  $n$ -alkane liquids is zero, the inverse Debye screening length  $\kappa$  is also zero, which means that  $C_{rf} = 0$  in (2).

In the GROMOS force field, the general van der Waals parameters  $C_{12}(i, j)$  and  $C_6(i, j)$  and the third-neighbour van der Waals parameters

$CS_{12}(i,j)$  and  $CS_6(i,j)$  are defined separately for each pair of atom types. It is possible within the GROMOS force field to parametrise self-interactions (between pairs of identical atoms) separately from crossed interactions (between different atom types). The force field doesn't depend on a given set of combination rules, which adds considerable flexibility to the parametrisation. By default, however, the parameters for crossed interactions are generated by taking the geometric mean of the self-interaction values:  $C_{12}(i,j) = [C_{12}(i,i) \cdot C_{12}(j,j)]^{1/2}$  and  $C_6(i,j) = [C_6(i,i) \cdot C_6(j,j)]^{1/2}$ , and likewise for the third-neighbour van der Waals parameters  $CS_{12}(i,j)$  and  $CS_6(i,j)$ . Improvement of the *trans-gauche* ratio for aliphatic carbon chains or *n*-alkanes only involves a refitting of the torsional angle interaction parameter  $K_{\varphi_n}$  for dihedrals of type  $\square-\text{CH}_n-\text{CH}_n-\square$  and of the third-neighbour van der Waals parameters  $CS_{12}(\text{CH}_2, \text{CH}_2)$ ,  $CS_{12}(\text{CH}_3, \text{CH}_3)$ ,  $CS_6(\text{CH}_2, \text{CH}_2)$  and  $CS_6(\text{CH}_3, \text{CH}_3)$ . It turned out that the latter two parameters could be kept at their GROMOS96 43A1 values while varying the other three parameters to fit the calculated liquid energy, pressure and *trans-gauche* ratio for the three *n*-alkanes to the target values given in Table II.

The GROMOS96 software [11] was used in all simulations. For the investigation of liquid alkane properties, 512 molecules ( $= N_{\text{molecule}}$ ) have been used within a cubic box under periodic boundary conditions. The box length  $l_{\text{box}}$  chosen corresponds to the experimental density at 298.15 K of the liquid ( $\rho_{\text{liquid}}$ ) and is calculated through Eq. (3) leading to 4.41814 nm for *n*-butane, 4.62264 nm for *n*-pentane and 4.80535 nm for *n*-hexane.

$$l_{\text{box}} = \left( \frac{N_{\text{molecule}} \cdot M_{\text{molecule}}}{\rho_{\text{liquid}}} \right)^{1/3}, \quad (3)$$

where  $M_{\text{molecule}}$  is the mass of an *n*-alkane molecule. Starting from a regular array of molecules, a molecular dynamics simulation at constant volume and temperature (NVT) of 500 ps was carried out. Initial velocities were taken from a Maxwellian distribution at 298.15 K and the initial centre of mass motion was removed. The time coupling constant for coupling to the temperature bath was set to  $\tau_T = 0.1$  ps [44]. The time step used in the leap-frog integration scheme was 0.002 ps. Except for bond constraints maintained at a relative geometrical tolerance of  $10^{-4}$  by the SHAKE algorithm [45] all internal interactions were treated explicitly. A twin range cutoff of 0.8/1.4 nm was applied to the non-bonded interactions and the non-bonded pairlist and the long-range forces were updated every 5 time steps.

TABLE II Comparison of properties for different combinations of force field parameters. GROMOS96 third-neighbour non-bonded and dihedral angle potential parameters were tested using *n*-alkane simulations. New parameter sets (a to d) were used to improve the dihedral angle potential energy profiles (Fig. 2). Results have been compared to OPLS united-atom and all-atom approaches. Reference values for experimental heat of vaporization and pressure are found in [17], those for the percentages of *trans* configuration are interpolated from [24, 29, 31, 43] for *n*-butane, from [24, 29] for *n*-pentane and from [29] for *n*-hexane, where the value in parentheses is an average measured for longer *n*-alkanes also from [29]

Forcefield		Parameters			Properties				
Name, interaction	$K_{\varphi_n}$	Dihedral potential $\delta_n$	$m_n$	1-4 van der Waals parameters $CS_{12}(CH_3, CH_3)$	$CS_6(CH_3, CH_3)$	$\Delta H_{vap}$ [kJ/mol]	$p$ [atm]	$r_{geom}$ [%]	Number of transitions [per dihedral per 100 ps]
Experimental target									
GROMOS96 43A1	5.86	+1	3	0.1206173E-04	0.6852528E-02	21.62	2.43	60	-
GROMOS96a	7.08	+1	3	0.6793766E-05	0.6852528E-02	20.76	130.13	91	1.72
GROMOS96b	6.28	+1	3	0.6412316E-05	0.6852528E-02	20.87	124.87	66	1.79
GROMOS96c 43A2	5.92	+1	3	0.6030863E-05	0.6852528E-02	20.74	121.64	63	3.08
GROMOS96d	6.28	+1	3	0.6030863E-05	0.6852528E-02	21.00	121.77	60	3.79
OPLS ua	3.18402	+1	1	0.0	0.0	21.05	130.11	68	2.56
	-0.65898	-1	2						
	6.70904	+1	3						
OPLS aa	3.640080	+1	1	0.1866303E-05	0.1015252E-02	21.20	131.27	74	2.00
	-0.328444	-1	2						
	0.583668	+1	3						
<i>n</i> -Pentane, $CH_3 \cdots CH_2$									
Experimental target									
GROMOS96 43A1	5.86	+1	3	0.9262491E-05	0.5689469E-02	26.43	0.68	64	-
GROMOS96a	7.08	+1	3	0.5675873E-05	0.5689469E-02	26.30	40.92	86	2.41, 2.42
GROMOS96b	6.28	+1	3	0.5347702E-05	0.5689469E-02	26.12	31.39	69	1.92, 2.03
GROMOS96c 43A2	5.92	+1	3	0.5347702E-05	0.5689469E-02	26.47	35.76	66	3.15, 3.10
GROMOS96d	6.28	+1	3	0.5186203E-05	0.5689469E-02	26.09	24.64	66	3.74, 3.84
OPLS ua	2.95181	+1	1	0.0	0.0	26.25	39.90	72	2.71, 2.72
	-0.56693	-1	2						
	6.57934	+1	3						
OPLS aa	3.640080	+1	1	0.1866303E-05	0.1015252E-02	26.37	117.74	80	1.64, 1.64
	-0.328444	-1	2						
	0.583668	+1	3						



TABLE II (Continued)

Forcefield Name, interaction <i>n</i> -Hexane, CH <sub>2</sub> —CH <sub>2</sub>	Parameters			Properties			Number of transitions [per dihedral per 100 ps]		
	Dihedral potential K <sub>φ<sub>n</sub></sub>	δ <sub>n</sub>	m <sub>n</sub>	1-4 van der Waals parameters CS <sub>12</sub> (CH <sub>2</sub> , CH <sub>2</sub> )	CS <sub>6</sub> (CH <sub>2</sub> , CH <sub>2</sub> )	ΔH <sub>vap</sub> [kJ/mol]		<i>p</i> [atm]	<i>r</i> <sub>geom</sub> [%]
Experimental target						<b>31.55</b>	<b>0.20</b>	<b>65(66)</b>	—
GROMOS96 43A1	5.86	+1	3	0.7112889E-05	0.4723813E-02	31.87	31.12	86, 80, 86	2.33, 3.38, 2.37
GROMOS96a	7.08	+1	3	0.4741926E-05	0.4723813E-02	31.80	-3.72	67, 71, 67	2.36, 1.94, 2.30
GROMOS96b	6.28	+1	3	0.4459842E-05	0.4723813E-02	31.78	9.35	65, 68, 65	3.64, 3.05, 3.59
GROMOS96c 43A2	5.92	+1	3	0.4741926E-05	0.4723813E-02	31.63	0.44	63, 71, 63	4.39, 3.60, 4.39
GROMOS96d	6.28	+1	3	0.4459842E-05	0.4723813E-02	31.70	2.10	63, 69, 63	3.58, 3.06, 3.56
OPLS ua	2.95181	+1	1	0.0	0.0	32.07	4.08	70, 77, 70	3.05, 2.55, 3.07
	-0.56693	-1	2						
	6.57934	+1	3						
OPLS aa	3.640080	+1	1	0.1866303E-05	0.1015252E-02	32.07	166.02	80, 84, 80	1.51, 1.27, 1.41
	-0.328444	-1	2						
	0.583668	+1	3						

The trajectories of configurations were used after 100 ps of equilibration time to calculate the average energy, the average pressure, the geometric *trans-gauche* ratio (Eq. (4)), and the number of transitions of dihedral angles, from which both the frequency of transition and the transition-derived *trans-gauche* ratio (Eq. (5)) can be calculated. The geometric definition of the percentage of *trans* conformations depends on the number of *trans* configurations  $n_{\varphi_t}$  and the number of *gauche* configurations  $n_{\varphi_g}$  in the trajectory:

$$\langle r_{\text{geom}} \rangle = \frac{\sum n_{\varphi_t} \cdot 100}{\sum n_{\varphi_t} + \sum n_{\varphi_g}}, \quad \text{for } \begin{cases} \varphi = \{-180^\circ \dots +180^\circ\} \\ \varphi_t = |\varphi| > 120^\circ \\ \varphi_g = |\varphi| < 120^\circ \end{cases} \quad (4)$$

The geometric *trans-gauche* ratio is obtained by defining the top of the *trans-gauche* torsional energy barrier ( $\varphi = \pm 120^\circ$ ) as the separation line. In the same vein, one could define a dihedral angle transition to occur if the dihedral angle passes this barrier. However, if the dihedral angle immediately returns backwards over the barrier, one would not consider such crossing events as two transitions. Therefore, for the dihedral transitions, the definition used in the GROMOS package was applied [11]. A dihedral transition is only considered to be completed if the dihedral angle passes the bottom of an adjacent well in the dihedral energy term (1). Then the time difference  $\Delta t_{\varphi_t}$  between two subsequent transitions from and to the *trans* configuration and the corresponding time difference  $\Delta t_{\varphi_g}$  can be used to define a transition-derived percentage of *trans* conformations:

$$\langle r_{\text{trans}} \rangle = \frac{\sum \Delta t_{\varphi_t} \cdot 100}{\sum \Delta t_{\varphi_t} + \sum \Delta t_{\varphi_g}}, \quad \begin{cases} \Delta t_{\varphi_t} = t_{\varphi_t} \rightarrow t_{\varphi_g} \\ \Delta t_{\varphi_g} = t_{\varphi_g} \rightarrow t_{\varphi_t} \end{cases} \quad (5)$$

Time differences in Eq. (5) have been taken from the registered transitions of the dihedral angles of the same type. In all cases, the transition-derived average *trans-gauche* ratios are within 10% of the average geometrical *trans-gauche* ratios. For the parametrisation, only the geometrical *trans-gauche* ratios have been taken into account and only this data is shown in Table II.

To calculate the heat of vaporization simulations in vacuum are required. The final coordinates and velocity vectors of the liquid simulation trajectory have been used to initialise simulations in vacuum. The 512 molecules were redistributed into a much larger box of 400 nm side length to avoid intermolecular interactions. With this large cubic box and a single cutoff of 1.0 nm, a vacuum trajectory of 100 ps was produced (50 ps equilibration time). From the potential energies  $E_{\text{pot}}$  of the liquid and

vacuum simulations the heat of vaporization for the pure substance was calculated using Eq. (6) which simply corresponds to the enthalpy difference  $H_{\text{gas}} - H_{\text{liquid}}$ . The average total potential molecular energy of the liquid phase is subtracted from the average total potential molecular energy lacking the intermolecular contacts in the gas phase under the assumption of ideality in the gas using  $RT$  replacing  $pV$ ,

$$\Delta H_{\text{vap}} = E_{\text{pot}}(g) - E_{\text{pot}}(l) + RT. \quad (6)$$

#### 4. RESULTS AND DISCUSSION

The van der Waals repulsive parameter  $CS_{12}$  of the GROMOS96 43A1 force field shows a too large repulsion between third neighbours in the energy as function of dihedral angle for aliphatic chains. *n*-Butane shows the largest deviation in energy levels using the original GROMOS96 parameters.

As can be seen in Table II, the simulated percentage of *trans* conformers is too large, 91, 86 and (86, 80, 86) percent for the three *n*-alkane liquids as compared to the target values of 60, 64 and 65 percent, respectively. The *trans-gauche* ratio can be reduced by decreasing the third-neighbour repulsive van der Waals parameters  $CS_{12}$ . This decrease will also reduce the *trans/gauche* energy barriers which can be counteracted by increasing the force constant of the torsional angle energy term  $K_{\varphi_n}$ . These parameter changes will also affect the heat of vaporization and the pressure of the liquids. A large number of parameter value combinations was tested. The results for a few of these are shown in Table II. The amplitude of the dihedral potential energy term was either set to fit the barrier height of *n*-hexane (models b, c and d) or *n*-butane (model a). This affects the kinetics of dihedral transitions and in the case of *n*-hexane changed the molecular kinetics completely: the central dihedral is less mobile than the end dihedral angles. Large deviations in the heat of vaporization were not observed using the new models a to d, but the sampling of dihedral space is indeed different compared to GROMOS96 43A1 and also the pressure was positively affected. The modification indicated by the symbol GROMOS96c yields the best agreement with the nine target values. Compared to the GROMOS96 43A1 results these parameters yield a significant improvement of the *trans-gauche* ratio, while agreeing even slightly better with the target values for the heat of vaporization and pressure.

Table II also contains values for the OPLS united-atom [12, 47] and all-atom [13, 46, 48] force fields. The OPLS united-atom parameters which are

relatively old, yield surprisingly good agreement with the target values, which were partially not yet available in 1984. The much newer OPLS all-atom model produces too high pressures and too large *trans-gauche* ratios.

The OPLS parameters originate from (N, P, T) Monte Carlo simulations using a 1.1 nm intermolecular non-bonded cut-off in the all-atom case [46] and values in the range of 0.95 to 1.5 nm in the united-atom case [47]. When fitting the OPLS force field parameters, a correction was made that approximately accounts for the non-bonded interactions between atom pairs at a distance larger than the cut-off distance ( $R_c$ ). We have analysed the size of these long-range contributions to the energy and pressure as a function of cut-off radius in the appendix. The results for the three *n*-alkanes using GROMOS96 and OPLS force fields with a cut-off radius of 1.4 nm are shown in Table III. The contribution of forces beyond  $R_c = 1.4$  nm enlarges the heat of vaporization by at most  $1 \text{ kJ mol}^{-1}$  and reduces the pressure by maximally 150 atm. Inclusion of the long-range contribution improves the agreement with experiment for *n*-butane, while for *n*-pentane and *n*-hexane the heat of vaporization becomes too large. For the latter

TABLE III 1.4 nm cut-off contribution correction to heat of vaporization and pressure for *n*-alkanes. Heat of vaporization and pressure from MD simulations using a non-bonded cut-off radius  $R_c = 1.4$  nm and the corresponding contributions  $E_{R_c}$  and  $p_{R_c}$  calculated using Eqs. (A.8) and (A.9). All simulation results have been obtained with the GROMOS96 program [11]. For further explanation see captions of Tables II, IV–VI and the methods section

	<i>n</i> -Butane		<i>n</i> -Pentane		<i>n</i> -Hexane	
	$\Delta H_{vap}$ $\text{kJ mol}^{-1}$	$p$ $\text{atm}$	$\Delta H_{vap}$ $\text{kJ mol}^{-1}$	$p$ $\text{atm}$	$\Delta H_{vap}$ $\text{kJ mol}^{-1}$	$p$ $\text{atm}$
<i>Experiment</i>	21.62	2.4	26.43	0.68	31.55	0.20
<b>GROMOS96 (43A1)</b>						
MD	20.76	130	26.30	41	31.87	31
$-E_{R_c}, p_{R_c}$	0.61	-119	0.81	-137	1.01	-153
sum	21.37	11	27.11	-96	32.88	-122
<b>GROMOS96 (43A2)</b>						
MD	21.00	122	26.09	25	31.63	0
$-E_{R_c}, p_{R_c}$	0.61	-119	0.81	-137	1.01	-153
sum	21.61	3	26.90	-112	32.64	-153
<b>OPLS-UA</b>						
MD	21.05	130	26.25	40	32.07	4
$-E_{R_c}, p_{R_c}$	0.62	-121	0.82	-139	1.02	-154
sum	21.67	9	27.07	-99	33.09	-150
<b>OPLS-AA</b>						
MD	21.20	131	26.37	118	32.07	166
$-E_{R_c}, p_{R_c}$	0.38	-75	0.51	-86	0.64	-96
sum	21.58	56	26.88	32	32.71	70

two liquids the pressure becomes too low for the united-atom models and it is still a bit too high for the OPLS all-atom model.

We note that the evaluation of the long-range contributions from pairs beyond the cut-off distance using Eqs. (A.8 – 9) is only possible for systems with an isotropic and homogeneous distribution in space of the different types of atom pairs, such as pure liquids or simple mixtures. For proteins and DNA in aqueous solution or membranes, such contributions cannot be estimated using (A.8 – 9), but should be explicitly calculated. The GROMOS96 force field has therefore been parametrised using a relatively long cut-off of 1.4 nm and without any corrections of the type of Eqs. (A.8 – 9). This 1.4 nm cut-off radius is thus a parameter of the GROMOS96 force field. When comparing results in Table III, the pure MD-simulation results should be used for GROMOS96, whereas the long-range contributions  $-E_{R_c}$  and  $p_{R_c}$  should be included for OPLS. For *n*-butane the OPLS results agree better than the GROMOS96 ones with experiment, whereas for *n*-pentane and *n*-hexane the GROMOS96 results are better than both OPLS united-atom and all-atom results. This illustrates the observation that a more complex model need not necessarily give better results than a simple model. One should note that for proteins an all-atom model almost quadruples the number of non-bonded interactions to be calculated compared to a united-atom model. For membrane simulations the computational effort will be increased by an even larger factor.

## 5. CONCLUSIONS

The dihedral angle energy parameter  $K_{\varphi_n}$  for dihedral angles of type  $\square-\text{CH}_n-\text{CH}_n-\square$  and the third-neighbour van der Waals repulsive parameters for atom types  $\text{CH}_2$  and  $\text{CH}_3$  of the GROMOS 43A1 set of force field parameters have been modified to better fit the heat of vaporization, pressure and *trans-gauche* ratio for liquid *n*-butane, *n*-pentane and *n*-hexane. The new parameter set, denoted GROMOS 43A2 yields significantly better results than the 43A1 set.

When comparing the mentioned properties calculated using OPLS united-atom force field parameters and OPLS all-atom force field parameters with the GROMOS 43A2 parameters, the OPLS force fields perform better for *n*-butane, whereas the GROMOS96 force field does better for *n*-pentane and *n*-hexane. This illustrates that a more complex and time consuming (all-atom) model need not necessarily yield better results than

a simple (united-atom) one. This finding suggests that the efficiency of biomolecular simulation will benefit from the use and development of united-atom models.

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## APPENDIX

### Energy and Pressure Corrections for Finite Cut-off

The use of a cut-off radius ( $R_c$ ) for non-bonded interactions in a molecular simulation is only allowed if the contribution of the forces between atoms at a distance larger than  $R_c$  is negligible, or if a good approximation of these forces can be formulated. For a homogeneous atomic liquid the contribution of atom pairs at a distance beyond  $R_c$  to the potential energy is [49].

$$E_{R_c} = 2\pi N_{\text{at}}^2 V^{-1} \int_{R_c}^{\infty} r^2 V^{\text{nonb}}(r) g(r) dr, \quad (\text{A.1})$$

and to the pressure it is

$$p_{R_c} = -\frac{1}{3} 2\pi N_{\text{at}}^2 V^{-2} \int_{R_c}^{\infty} r^2 \left( r \frac{dV^{\text{nonb}}}{dr} \right) g(r) dr. \quad (\text{A.2})$$

The number of atoms in the volume  $V$  is  $N_{\text{at}}$ ,  $V^{\text{nonb}}(r)$  is the non-bonded atom–atom interaction, and  $g(r)$  is the atom–atom radial distribution function. The integrals in (A.1) and (A.2) can be calculated when  $V^{\text{nonb}}(r)$  and  $g(r)$  are known. For a non-bonded interaction of Lennard-Jones type,

$$V^{\text{nonb}}(r) = \frac{C_{12}}{r^{12}} - \frac{C_6}{r^6} \quad (\text{A.3})$$

and for large values of  $R_c$  one may use the approximations

$$V^{\text{nonb}}(r) = -C_6 r^{-6} \quad (\text{A.4})$$

and

$$g(r) = 1. \quad (\text{A.5})$$

Then one obtains for a system of  $N_{\text{at}}$  atoms

$$E_{R_c} = -\frac{2\pi N_{\text{at}}^2 C_6}{3 V R_c^3} \quad (\text{A.6})$$

and

$$p_{R_c} = -\frac{4\pi}{3} \left( \frac{N_{\text{at}}}{V} \right)^2 \frac{C_6}{R_c^3} = 2E_{R_c} V^{-1}. \quad (\text{A.7})$$

For a system of  $N_{\text{molecule}}$  molecules, each consisting of  $N_{\text{am}}$  atoms per molecule, the value of  $E_{R_c}$  per molecule is

$$E_{R_c}^{\text{mol}} = -\frac{2\pi N_{\text{at}} C_6}{3 V R_c^3} N_{\text{am}} \quad (\text{A.8})$$

and

$$p_{R_c} = 2E_{R_c}^{\text{mol}} V^{-1} N_{\text{molecule}}. \quad (\text{A.9})$$

The expressions  $E_{R_c}^{\text{mol}}$  and  $p_{R_c}$  were evaluated for the homogeneous systems of *n*-butane, *n*-pentane and *n*-hexane using cut-off radii  $R_c$  ranging from 0.8 to 1.8 nm and  $C_6$  parameters from the GROMOS96 and OPLS force fields. The  $C_6$  parameters are listed in Table IV. Since the *n*-alkanes contain two types of atoms,  $\text{CH}_2$  and  $\text{CH}_3$  in the united-atom representation,

TABLE IV Lennard-Jones  $C_6$  attractive parameters for intermolecular non-bonded interactions. Attractive intermolecular non-bonded interaction parameters  $C_6$  (see Eq. (2)), in  $\text{kJ mol}^{-1} \text{nm}^6$ , for alkanes or aliphatic chains in the GROMOS96 (43A1, 43A2) [11], OPLS united atom (UA) [47] and OPLS all-atom (AA) [46] force fields

Pair type	Force field GROMOS96	Force field OPLS-UA	Pair type	Force field OPLS-AA
$\text{CH}_2-\text{CH}_2$	0.007105	0.007003	C—C	0.00203050
$\text{CH}_2-\text{CH}_3$	0.008394	0.008528	C—H	0.00049889
$\text{CH}_3-\text{CH}_3$	0.009916	0.010385	H—H	0.00012258

and C and H in the all-atom representation, the  $C_6$  value used in Eqs. (A.8 – 9) is a weighted sum of the  $C_6$  values of each type of atom pair with the fraction of each pair type given in Table V as weight factor. Table VI contains the heat of vaporization and pressure as obtained from MD simulations, and the values of expressions (A.8) and (A.9) for different cut-off radii  $R_c$ . Beyond  $R_c = 1.4$  nm the long-range contributions become rather small compared to other approximations inherent to the force fields. Below  $R_c = 1.0$  nm, the assumptions of homogeneity (generally a charge-group or molecular cut-off is used in biomolecular force fields), and Eq. (A.5) become incorrect, especially for the larger  $n$ -hexane.

The OPLS parameters have been obtained by fitting of the heat of vaporization and the density of  $n$ -alkanes in (N, P, T) Monte Carlo simulations of the liquids [46, 47]. It is explicitly stated in [46, 47] that the contribution  $E_{R_c}$  to the energy was included in the fitting of the heat of vaporization. However, nothing is stated in [46, 47] about inclusion of the corresponding contribution  $p_{R_c}$  to the pressure when fitting to the experimental density.

When deriving the force field parameters of the GROMOS96 force field, the contributions  $E_{R_c}$  and  $p_{R_c}$  were not considered [14], since a relatively long cut-off radius  $R_c = 1.4$  nm was used for both the electrostatic and van der Waals interactions, which makes these contributions rather small.

TABLE V Densities of molecules, atoms and pairs of atoms of different types. For further explanation see text of methods section and the appendix

	<i>n-Butane</i>	<i>n-Pentane</i>	<i>n-Hexane</i>
Box volume [nm <sup>3</sup> ]	86.2419	98.7803	110.9620
Number of molecules in box [ $N_{\text{molecule}}$ ]	512	512	512
Number of atoms			
per molecule [ $N_{\text{am}}$ ]:			
united-atom models (CH <sub>2</sub> , CH <sub>3</sub> )	4(2, 2)	5(3, 2)	6(4, 2)
all-atom models (C, H)	14(4, 10)	17(5, 12)	20(6, 14)
in box [ $N_{\text{at}}$ ]:			
united-atom models	2048	2560	3072
all-atom models	7168	8704	10240
Fraction of atom pairs of types			
for united-atom models:			
CH <sub>2</sub> —CH <sub>2</sub>	4/16	9/25	16/36
CH <sub>2</sub> —CH <sub>3</sub>	8/16	12/25	16/36
CH <sub>3</sub> —CH <sub>3</sub>	4/16	4/25	4/36
for all atom models:			
C—C	16/196	25/289	36/400
C—H	80/196	120/289	168/400
H—H	100/196	144/289	196/400





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